

Is there a version of Private Eye for Linux?

No. The idea of Protected Storage is specific to Microsoft Windows.